

DIFFERENTIATION RULES

Let α , b , k , and r be constants, with $b > 0$, $b \neq 1$, and $f, g : \mathbb{R} \rightarrow \mathbb{R}$ differentiable functions. Then:

TERMINAL RULES

Rules of differentiation that **resolve** a derivative in a form that does not require further differentiation.

$$(1) \frac{d}{dx} \{k\} =$$

$$(2) \frac{d}{dx} \{x^\alpha\} =$$

$$\bullet \frac{d}{dx} \{x\} =$$

$$\bullet \frac{d}{dx} \left\{ \frac{1}{x^\alpha} \right\} =$$

$$(3) \frac{d}{dt} \{e^{rt}\} =$$

$$\bullet \frac{d}{dx} \{b^x\} =$$

$$(4) \frac{d}{dx} \{\sin x\} =$$

$$(5) \frac{d}{dx} \{\cos x\} =$$

$$(6) \frac{d}{dx} \{\tan x\} =$$

$$(7) \frac{d}{dx} \{\arcsin x\} =$$

$$(8) \frac{d}{dx} \{\arccos x\} =$$

$$(9) \frac{d}{dx} \{\arctan x\} =$$

$$(10) \frac{d}{dx} \{\ln x\} =$$

$$\bullet \frac{d}{dx} \{\log_b x\} =$$

NONTERMINAL RULES

Rules of differentiation that expresses a derivative of a function in terms of derivatives of **simpler** functions.

$$(11) \frac{d}{dx} \{k \cdot f(x)\} =$$

$$(12) \frac{d}{dx} \{f(x) \pm g(x)\} =$$

$$(13) \frac{d}{dx} \{f(x) \cdot g(x)\} =$$

$$(14) \frac{d}{dx} \left\{ \frac{f(x)}{g(x)} \right\} =$$

$$\bullet \frac{d}{dx} \left\{ \frac{k}{g(x)} \right\} =$$

$$\bullet \frac{d}{dx} \left\{ \frac{f(x)}{k} \right\} =$$

$$(15) \frac{d}{dx} \{f(g(x))\} =$$

$$(16) \frac{d}{dy} \{f^{-1}(y)\} =$$